This article was downloaded by: On: 24 January 2011 Access details: Access Details: Free Access Publisher Taylor & Francis Informa Ltd Registered in England and Wales Registered Number: 1072954 Registered office: Mortimer House, 37-41 Mortimer Street, London W1T 3JH, UK



### Journal of Macromolecular Science, Part A

Publication details, including instructions for authors and subscription information: http://www.informaworld.com/smpp/title~content=t713597274

## Dependence of Polymer Chain Entanglements on the Solution Concentration

H. U. Khan<sup>a</sup>; K. K. Bhattacharyya<sup>a</sup> <sup>a</sup> Indian Institute of Petroleum, Dehradun, India

To cite this Article Khan, H. U. and Bhattacharyya, K. K.(1987) 'Dependence of Polymer Chain Entanglements on the Solution Concentration', Journal of Macromolecular Science, Part A, 24: 7, 841 — 852 To link to this Article: DOI: 10.1080/00222338708082099 URL: http://dx.doi.org/10.1080/00222338708082099

## PLEASE SCROLL DOWN FOR ARTICLE

Full terms and conditions of use: http://www.informaworld.com/terms-and-conditions-of-access.pdf

This article may be used for research, teaching and private study purposes. Any substantial or systematic reproduction, re-distribution, re-selling, loan or sub-licensing, systematic supply or distribution in any form to anyone is expressly forbidden.

The publisher does not give any warranty express or implied or make any representation that the contents will be complete or accurate or up to date. The accuracy of any instructions, formulae and drug doses should be independently verified with primary sources. The publisher shall not be liable for any loss, actions, claims, proceedings, demand or costs or damages whatsoever or howsoever caused arising directly or indirectly in connection with or arising out of the use of this material.

# NOTE DEPENDENCE OF POLYMER CHAIN ENTANGLEMENTS ON THE SOLUTION CONCENTRATION

H. U. KHAN and K. K. BHATTACHARYYA

Indian Institute of Petroleum Dehradun 248005, India

#### INTRODUCTION

For the viscometric determination of molecular weights of polymers, sufficiently dilute solutions have to be used so that entanglements of the polymer chain are absent. The concentration of the polymer should be such that the relative viscosity  $(\eta_r)$  lies in the range 1.1-1.5 [1]. Similarly, for molecular weight determination by light scattering, the suggested concentration for polymer with weight-average molecular weight  $(\overline{M}_w) > 10^5$  is 0.5 wt%; for those with  $\overline{M}_w < 10^5$ , up to 1% may be used [2].

The limits of polymer concentration for such measurements are not clearly known. On dissolution, the polymer molecules adopt a more or less extended configuration whose shape depends on the structure and molecular weight of the polymer, the properties of the solvent, and the temperature [3]. The molecules of flexible linear polymers acquire a coiled configuration due to free rotation about the C-C bonds. When a dilute solution satisfies theta conditions, the polymer molecules are free from all kinds of interaction and move freely. Then their solution properties could possibly be related to their end-to-end distance. Based on this concept, our attempt to establish the permissible limits of polymer concentration for dilute solutions of several polymers of different molecular weights is reported here.

Copyright © 1987 by Marcel Dekker, Inc.

#### **THEORETICAL BASIS**

If C g of a polymer of molecular weight  $\overline{M}_n$  is dissolved in unit volume of solvent, and if each of these molecules is assumed to occupy the volume of a close-packed cuboid of side d, the following expression holds:

$$d^3 = \widehat{M}_n / C N_0 \tag{1}$$

where  $N_0$  is Avogadro's number. At low concentration, the distance *d* is a measure of the molecular dimensions of the polymer and is related to hydrodynamic parameters, such as the root-mean-square end-to-end distance,  $\sqrt{\bar{r}^2}$ , of the polymer molecule. This is related to the intrinsic viscosity  $[\eta]$  and  $\overline{M}_n$  by the expression [4]

$$[\eta] = \phi \left(\sqrt{\bar{r}^2}\right)^3 / \overline{M}_n, \tag{2}$$

where  $\phi$ , barring a few exceptions [5, 6], is a constant and, as a good approximation, may be taken as  $2.71 \times 10^{21}$  [3].

In an unperturbed state, the end-to-end distance,  $\sqrt{\overline{r_0}^2}$ , obeys the expression  $\sqrt{\overline{r_0}^2} = \alpha \sqrt{\overline{r_0}^2}$ , where  $\alpha$  is the expansion factor. Under theta conditions,  $\alpha = 1$ , and in Eq. (2),  $[\eta]$  becomes  $[\eta]_{\theta}$  and  $\sqrt{\overline{r_0}^2}$  replaces  $\sqrt{\overline{r_2}}$ .

At constant  $\overline{M}_n$ , d decreases with increasing C (Eq. 1) and  $\sqrt{\overline{r_0}^2}$  increases with  $[\eta]/\alpha$  for nontheta solvents and with  $[\eta]_{\theta}$  for theta solvents. It may therefore be deduced that, at constant  $\overline{M}_n$ , the entanglements will occur when C reaches such a value that  $d \leq \sqrt{\overline{r_0}^2}$  or  $d \leq \alpha \sqrt{\overline{r_0}^2}$  under the theta or nontheta conditions, respectively. Under these conditions, C is denoted as  $C_{e\theta}$  or  $C_e$  (e = entanglement) expressed in g/mL. In the theta solvent we get, from Eqs. (1) and (2),

$$\left[\frac{\overline{M}_n}{C_{e\theta} N_0}\right]^{1/3} = \left[\frac{[\eta]_{\theta} \overline{M}_n}{\phi}\right]^{1/3}.$$
(3)

Substituting the numerical values for  $\phi$  and  $N_0$  and replacing  $[\eta]_{\theta}$  by  $K_{\theta} \bar{M}_n^{0.5}$ [1] in Eq. (3), we arrive at

$$C_{e\theta} = 0.4499/K_{\theta} \,\overline{M}_n^{0.5}.\tag{4}$$

Thus, at constant  $\overline{M}_n$ ,  $C_{e\theta}$  is inversely proportional to  $K_{\theta}$ , which is related to the molecular properties of the polymer in dilute solution.

#### POLYMER CHAIN ENTANGLEMENTS

For nontheta solvents, Eq. (4) becomes

 $C_e[\eta] = 0.4499.$ 

Here  $[\eta]$  is dependent on the structure of the polymer as well as the nature of the solvent and is, therefore, difficult to assign any specific value of  $C_e$ . On the other hand, in theta solvents, the state being unpurturbed,  $C_{e\theta}$  could be related to the structure of the polymer alone and, since  $K_{\theta}$  values are available in the literature, it became possible to evaluate the system for theta solvents.

#### **EVALUATION OF RESULTS**

The  $K_{\theta}$  values of polyolefins and vinyl, acrylic, and diene homopolymers were taken from the literature (Table 1). For polypropylene (PP), poly(1butene), poly(vinyl acetate) (PVAC), polystyrene (PS), and poly(methyl methacrylate) (PMMA), the  $K_{\theta}$  values are the average of those reported by different authors. The values of *d* for different molecular weights from 1 ×  $10^5$  to  $6 \times 10^5$  at constant *C*, e.g., 2.5, 5.0, 10, and 15 mg/mL, were calculated. Substitution of these data into Eq. (1) reveals that, at constant  $\overline{M}_n$ , *d* gradually decreases with increasing *C*. Substituting  $K_{\theta} \overline{M}_n^{0.5}$  for  $[\eta]_{\theta}$  in Eq. (2), for theta conditions,  $\sqrt{\overline{r_0}^2}$  was calculated for the four groups of polymers by taking the  $K_{\theta}$  values from Table 1. The results are for PP, poly(1-butene), and poly(isobutene) (PIB) shown in Fig. 1; similar plots for other polymers are not included here.

The dependence of  $\sqrt{\overline{r_0}^2}$  on  $K_\theta$  is shown in Fig. 2. It is interesting to note that, for  $\overline{M_n} = 1.0 \times 10^5$ , the plot is linear, while at higher  $\overline{M_n}$  it is no longer linear.

The  $C_{e\theta}$  values for different polymers calculated from  $K_{\theta}$  and  $\overline{M}_n$  following Eq. (4) are given in Table 2. Figure 3 illustrates the variation of  $C_{e\theta}$  with  $\overline{M}_n$  for four different homopolymers.

#### DISCUSSION

In Fig. 1 the curves of d intersect those of  $\sqrt{\overline{r_0}^2}$  for PP (1), poly(1-butene) (2), and PIB (3). Table 3 gives the values of C and  $\overline{M}_n$  corresponding to the intersecting point. The  $C_{e\theta}$  values corresponding to the  $\overline{M}_n$  of the intersecting points (in parentheses in Table 3) are found to be in good agreement with

(5)

Polymers	$K_{\theta} \times 1$	105
1. Polyolefins:		an gangan katangga kanangga katang nga katang ka
Polypropylene	174.2	(average of 182, 172, 168.5)
Poly(1-butene)	115.0	(average of 123, 107)
Poly(isobutene)	91.0	
2. Vinyl polymers:		
Poly(vinyl chloride)	156.0	
Poly(vinyl acetate)	85.0	(average of 90, 82, 78, 82, 92.9 101)
Polystyrene	77.0	(average of 82, 70, 76)
Poly(vinyl benzoate)	62.0	
3. Acrylic polymers:		
Poly(acrylic acid)	76.0	
Poly(methacrylic acid)	66.0	
Poly(methyl methacrylate)	59.3	(average of 50.5, 57.5, 63.1, 59.0, 58.0, 67.9)
4. Diene polymers:		
Polyisoprene (gutta percha)	232	
Polybutadiene (1,3)	185	
Polyisoprene (atactic)	119	

TABLE 1. Polymers and Their  $K_{\theta}$  Values [6]

the C values of the intersecting points. This confirms the validity of the above deductions. Thus, the data in Table 2 and 3 can be taken as guides for the upper concentration limits for determination of molecular weights under theta conditions.

Thus, under the theta conditions, the entanglement concentration is a combined function of the molecular weight and the structure of the molecules. The values of  $C_{e\theta}$  are different for different polymers of the same  $\overline{M}_n$ . This is

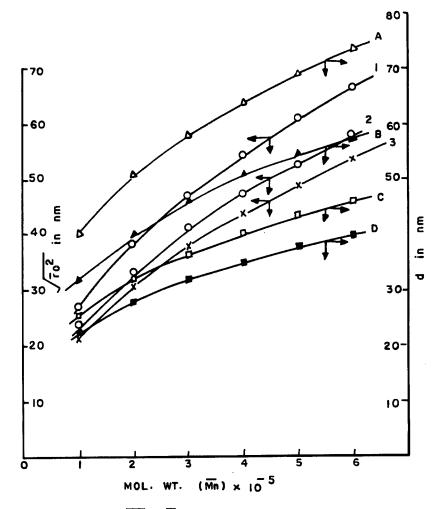
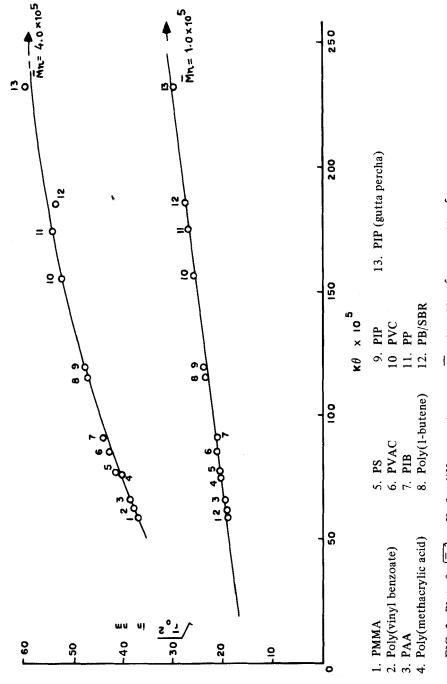


FIG. 1. Plot of  $\sqrt{\overline{r_0}^2}$  vs  $\overline{M_n}$  for different polyolefins and plot of d (in nm) vs  $\overline{M_n}$  at different concentrations, C, in g/mL. Curves 1 to 3 are, respectively, for PP, poly(1-butene), and PIB, whereas Curves A to D are at C of 2.5, 5.0, 10, and 15 mg/mL.





		Polyolefins	Vinyl polymers			
$\overline{M}_n \times 10^{-5}$	PP	Poly(1-butene)	PIB	PVC	PVAc	PS
0.5	1.143	1.750	2.196	1.2969	2.370	2.595
1.0	0.806	1.237	1.549	0.917	1.766	1.834
2.0	0.570	1.875	1.096	0.648	1.185	1.297
3.0	0.465	0.714	0.895	0.529	0.968	1.059
4.0	0.403	0.618	0.773	0.838	0.838	0.917
5.0	0.360	0.353	0.693	0.410	0.749	0.820
6.0	0.329	0.636	0.374	0.684	0.748	1.942

TABLE 2. Calculated Values of  $C_{e\theta}$  for Homopolymers<sup>a</sup>

	A	crylic p	olymers		Ľ	)iene polyn	ners
$\overline{M}_n \times 10^{-5}$	Poly(vinyl benzoate)	PAA	РМАА	РММА	PIP	<b>PB</b> (1,3)	PIP (atactic)
0.5	3.265	2.638	3.041	3.399	0.849	1.073	1.699
1.0	2.308	1.866	2.150	2.403	0.601	0.759	1.202
2.0	1.632	1.319	1.521	1.699	0.425	0.537	0.849
3.0	1.333	1.077	1.242	1.388	0.347	0.438	0.694
4.0	1.154	0.933	0.075	1.207	0.300	0.399	0.601
5.0	1.032	0.834	0.962	1.075	0.268	0.339	0.537
6.0	0.762	0.878	0.981	0.245	0.245	0.309	0.497

 ${}^{a}C_{e\theta} \times 10^{2}$  in g/mL.

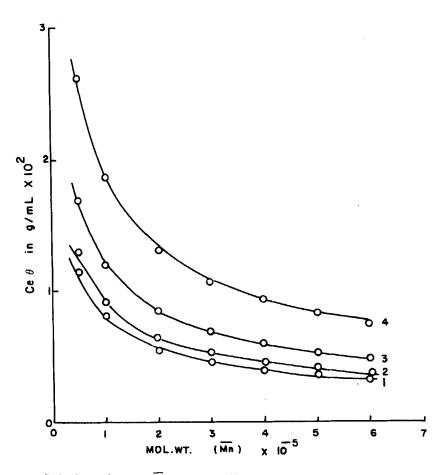


FIG. 3. Plot of  $C_{e\theta}$  vs  $\overline{M}_n$  for four different homopolymers: (1) PP, (2) PVC, (3) PIP, and (4) PAA.

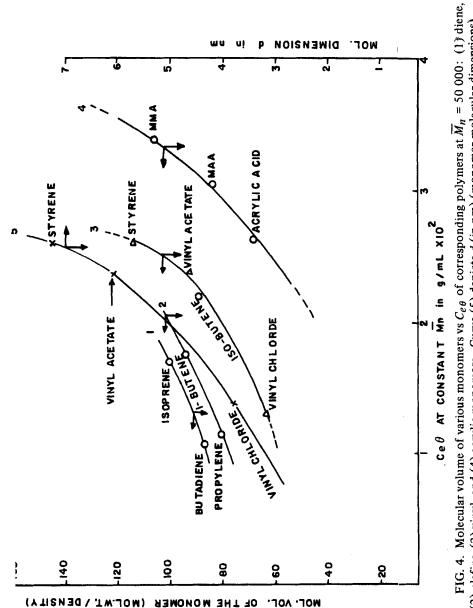
2011
January
24
18:28
At:
Downloaded

			T OID THE CISH A TH	T OT ATTACTS WITH JEVELS OF MAR AL THEESSCENTE PUTIT	א חוורזאברווו	ng punn		
X 10° g/mL	ЪР	Poly(	Poly(1-butene)	PIB	PVC	PVAc		PS
0.25						Í		-
0.50	250 000 (0.0050)	600 000	00	I	360 000 (0.0050)		·	ł
1.00	75 000 (0.0096)	190 000	00	250 000	85 000 (0.01)	180 000		325 000
1.50	I	75 000	00	I	**	120	120 000	165 000
Concentration			Polymers	Polymers with levels of $\overline{M}_n$ at intersecting point	$\overline{M}_n$ at interse	cting point		
$\times 10^{2} \text{ g/mL}$	Poly(vinyl benzoate)	zoate)	PAA	PMAA	PMMA	PIP .	PB (1,3)	PIP (atactic)
0.25	1		-		ł	285 000	1	1
0.50	I		1	I	ł	140 000	245 000	590 000 (0.0048)
1.00	580 000		340 000 (0.0102)	420 000	550 000	I	I	103 000 (0.0106)
1.50	260 000		150 000	190 000	270 000	I	I	Ι

## POLYMER CHAIN ENTANGLEMENTS

849

(Fig. 2).





Monomers	MW	Density <sup>a</sup>	Molecular volume, mL/mol	End-to-end distance, d, nm
Propylene	42.07	0.5139-20	81.86	3.81 2.99
1-Butene	56.104	0.5951	94.28	3.81
Isobutene	56.100	0.6266 <sup>-6.6</sup>	89.52	
Vinyl chloride	62.50	0.9918 <sup>-15</sup>	63.02	3.67
Vinyl acetate	86.09	0.9338	92.19	6.09 5.32
Styrene	104.14	0.9090 0.9075	114.57 114.75	7.24 6.54
Vinyl benzoate	148.0	_	_	-
Acrylic acid	72.06	1.0472 1.0511	68.81 68.56	
Methacrylic acid	86.09	1.0313	84.79	
Methyl methacrylate	100.11	0.936	106.96	5.81 6.81
Butadiene (1,3)	54.09	0.6211	87.09	5.48 4.96
Isoprene	68.11	0.6806	100.07	_
Vinyl butyrate	114.11	0.9022 0.8994	126.48 126.87	

TABLE 4. Molecular Dimensions (molecular volume and end-to-end distance) of Monomers

<sup>a</sup>At  $70^{\circ}$ C, except where noted otherwise.

in agreement with Eq. (4), confirming the validity of its derivation. The data in Table 2 and Fig. 3 allow two inferences to be drawn: 1) for a particular polymer,  $C_{e\theta}$  decreases with increasing  $\overline{M}_n$ ; and 2) at constant  $\overline{M}_n$ ,  $C_{e\theta}$  increases with decreasing  $K_{\theta}$ . The import of 1) for practical use is that the higher the  $\overline{M}_n$ , the lower should be the concentration.

Inference 2) indicates that for different polymers of the same  $\overline{M}_n$ ,  $\sqrt{\overline{r_0}^2}$  decreases with  $K_{\theta}$ , resulting in higher  $C_{e\theta}$  values. For rational correlation of these findings, the molecular volume and molecular dimension (end-to-end distance) of the monomers were calculated (Fig. 4 and Table 4). Though the curves in Fig. 4 are similar, their shape depends on the type of monomer. One unified curve relating  $C_{e\theta}$  for all these monomer parameters does not seem to be possible. However, such plots at different  $\overline{M}_n$  values would enable us to determine the  $C_{e\theta}$  values of the respective polymers.

#### ACKNOWLEDGMENTS

The authors thank Dr S. Bhattacharji for calculating the dimensions of the monomers and Dr P. S. N. Murthy for critically evaluating the revised manuscript.

#### REFERENCES

- F. W. Billmeyer, *Textbook of Polymer Science*, Wiley, New York, 1962, p. 81.
- [2] Instruction Manual, Phoenix Precision Co., Philadelphia, Pennsylvania, 1964, p. 22. A. Tayger, Physical Chemistry of Polymers, Mir, Moscow, 1972, p. 489.
- [3] D. A. Smith, Addition Polymers (Formation and Characterization), Plenum, New York, 1968, p. 208.
- [4] P. J. Flory and T. G Fox, J. Am. Chem. Soc., 73, 1904 (1951).
- [5] M. Kurata, W. H. Stockmayer, and A. Roig, J. Chem. Phys. 33, 151 (1960).
- [6] M. Kurata, M. Iwawa, and K. Kamada, in *Polymer Handbook* (J. Brandrup and E. Immergut, eds.), Wiley-Interscience, New York, 1966, p. IV-1-72.

Received March 20, 1986 Revision received September 22, 1986